

# UNDERSTANDING THE ROLES OF ROTATION, PULSATION AND CHEMICAL PECULIARITIES IN THE UPPER MAIN SEQUENCE

11th - 16th September 2016, Lake District, UK

## UNBIASED ESTIMATION OF A MULTIFREQUENCY SOLUTION IN DELTA SCUTI STARS

Javier Pascual Granado, Juan Carlos Suárez Yanes,  
Rafael Garrido Haba, and José Ramón Rodón



# STANDARD ANALYSIS PROCEDURE IN ASTEROSEISMOLOGY

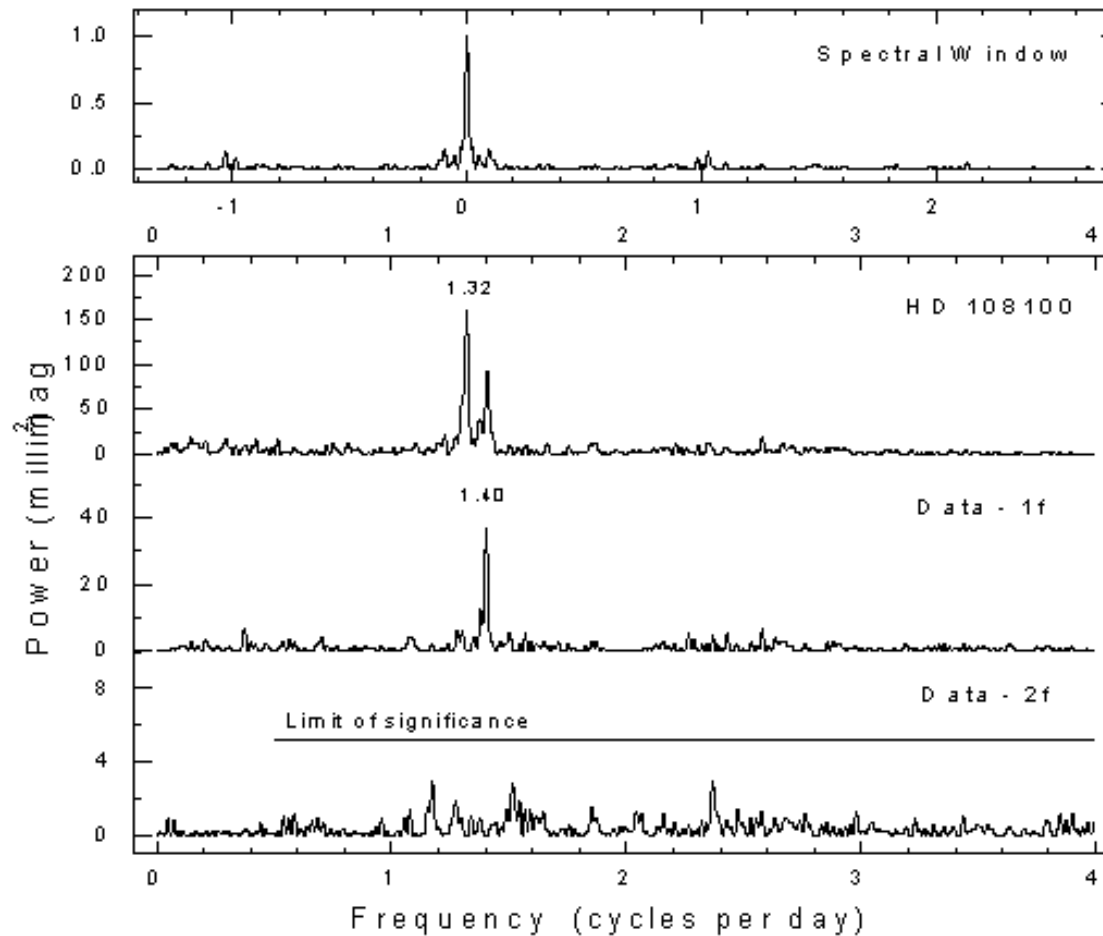
- Pre-processing: removal of systematics, outliers, de-trending, etc.
- Pre-whitening cascade – CLEAN method, SigSpec, etc.
- Filtering harmonics, combinations and/or spurious frequencies.
- Characterization of the spectrum:  $\Delta\nu$ ,  $\nu_{\max}$ ,  $\sigma$
- Model fitting

# PRE-WHITENING



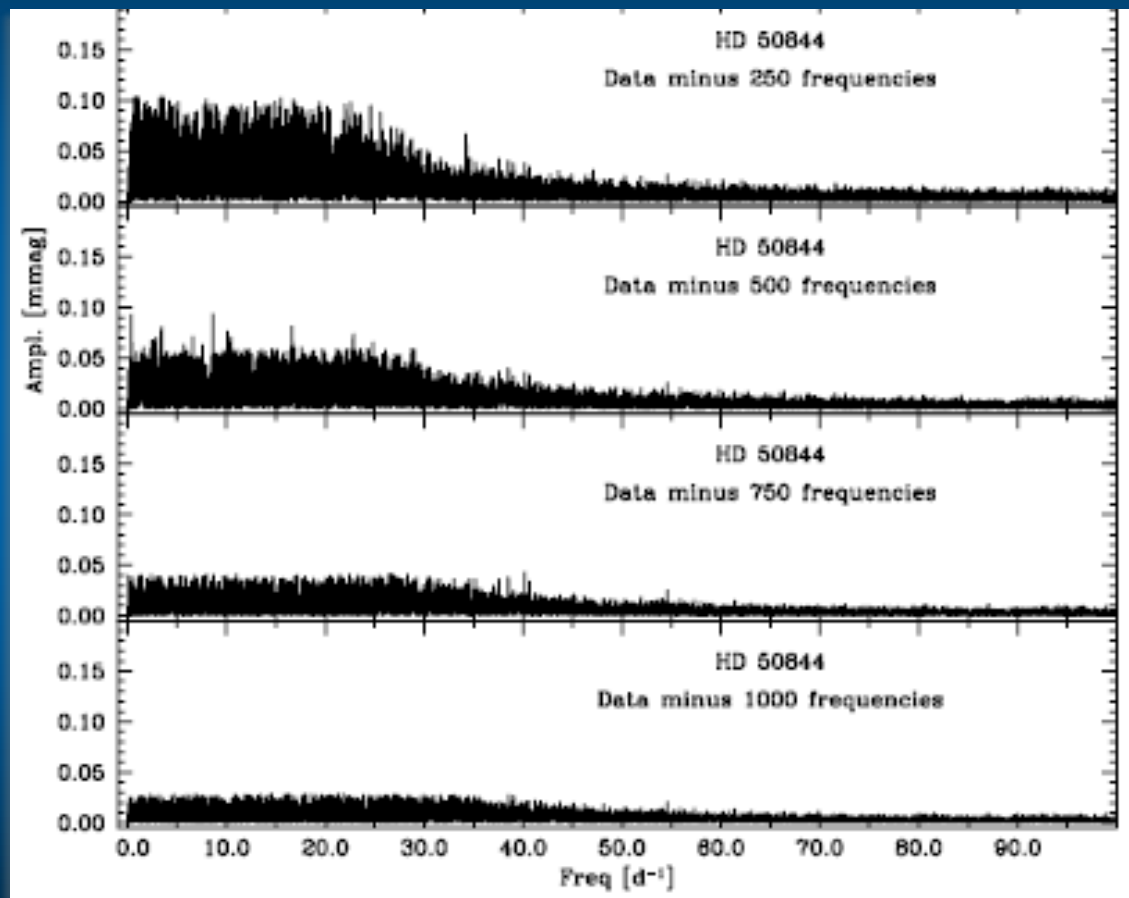
# PRE-WHITENING

Breger, M., Handler, G., Garrido, R., et al. 1996, DSN, 10, p.24



# HD 50844: an interpretation challenge

Poretti et al. 2009, A&A, 506, 85-93



- More than a thousands of frequencies detected.
- The residuals of the prewhitening sequence are not white noise (plateau)

**Also HD 50870, HD49434, ...**

# AIMS

## Impact of pre-whitening on frequency detection

- Gapped data
- ARMA interpolation: preserving the original frequency content  
Pascual-Granado, J., Garrido, R., and Suárez, J. C. 2015, A&A, 575, A78
- Linear interpolation: non-preserving the original frequency content

# THE SAMPLE

## CoRoT seismofield data. Why CoRoT?

CoRoT seismofield observations have  
~twice the cadence of Kepler SC

Advantages of higher cadence data:

- increased sampling rate
- higher Nyquist frequency
- fewer low-frequency artefacts
- **reduced errors on frequency, amplitude and phase determinations in the Fourier spectrum**

Murphy, Simon J., 2012, MNRAS, 422 (1), 665-671

# THE SAMPLE

Run	HD	ID	Star	SpT	mv	$\log T_{\text{eff}}$	$V$	$v \sin i$
IRa01	50844	123	A/F D Scu	A2	9.1	3,88	1,31	64
SRc01	174936	7613	A/F D Scu	A2	8.58	3,9	1,88	170
SRc01	174966	7528	A/F D Scu	A3	7.72	3,88	1,95	125
LRc01	181555	8669	A/F D Scu	A5 V	7.52	3,85	2,19	200
LRa01	49434	100	G Dor	F1 V	5.75	3,86	2,74	-
LRc02	172189	8170	A/F D Scu	A2	8.73	3,89	1	-
SRc02	174532	7655	A/F D Scu	A2	6.90	3,86	1,38	-
SRc02	174589	7663	A/F D Scu	F2 III	6.09	3,85	1,45	100
LRa02	51722	1022	A/F D Scu	A5	7.53	3,86	1,13	127
LRa02	51359	1320	A/F D Scu	A5	8.50	3,9	0,89	-
LRa02	50870	546	A/F D Scu	F0	8.88	3,88	1,67	17
LRc0506	170699	8301	A/F D Scu	A2	6,95	3,88	1,49	-
IRLRa04	GSC00144-03031	21960	A/F D Scu	A8	10,1	-	-	-
IRLRa05	41641	5685	A/F D Scu	A5	7,9	3,882	1,92	28
SRa05	48784	3619	A/F D Scu	F0	6,66	3,84	1,87	108



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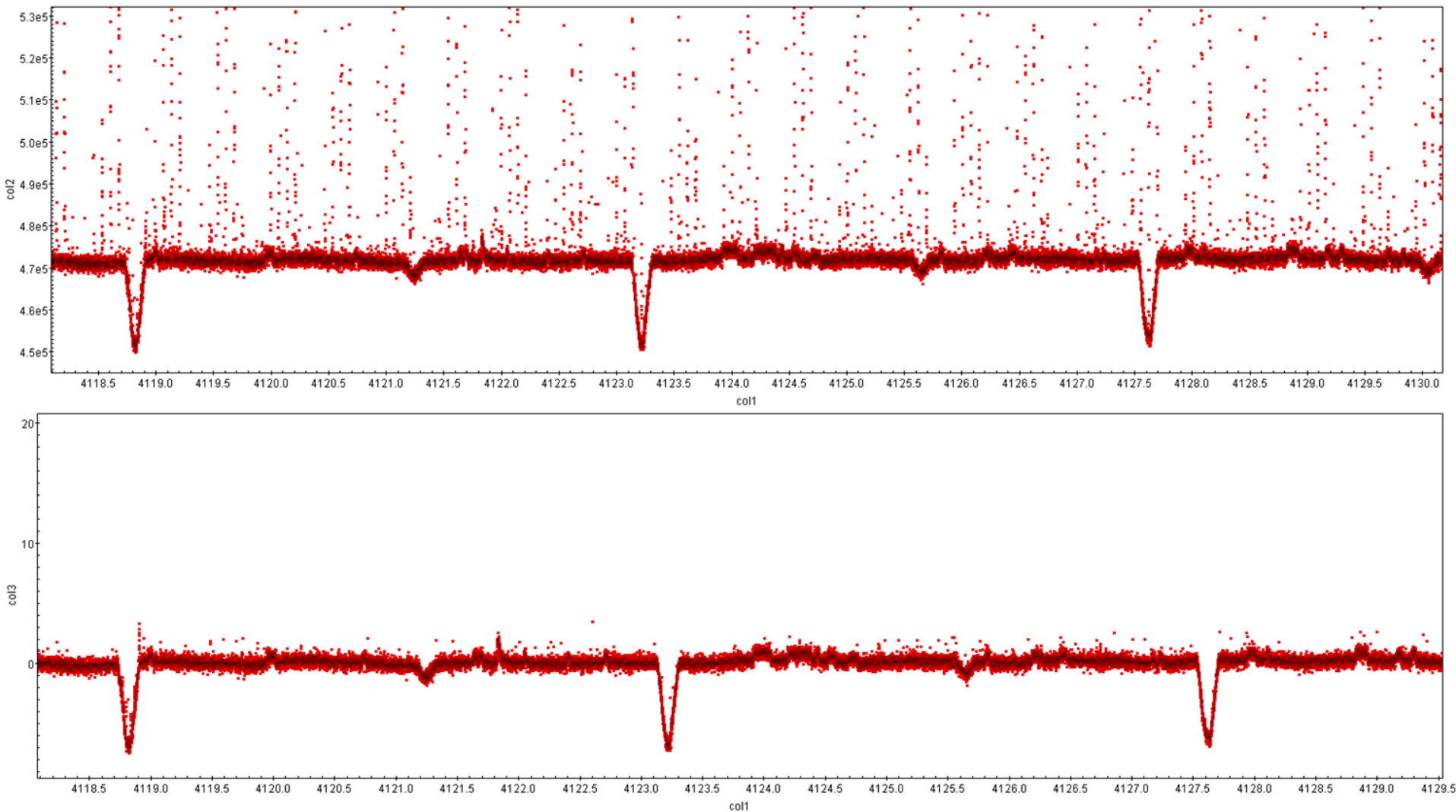
# AIMS

## Study of the impact of pre-whitening techniques used for frequency detection on asteroseismology

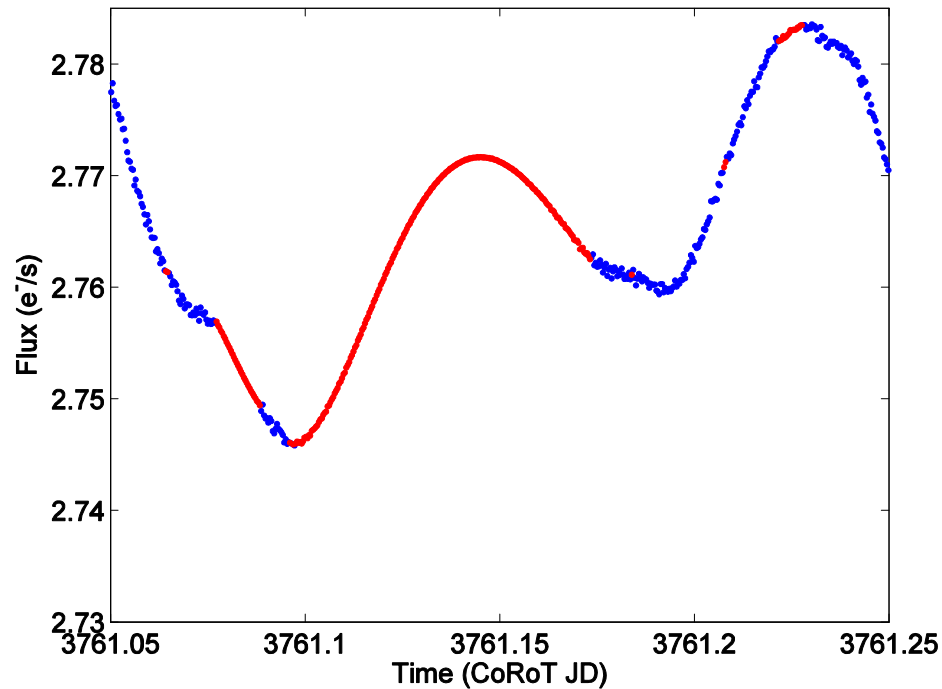
Three datasets are used:

- Gapped data
- ARMA interpolation: preserving the original frequency content  
Pascual-Granado, J., Garrido, R., and Suárez, J. C. 2015, A&A, 575, A78
- Linear interpolation: non-preserving the original frequency content

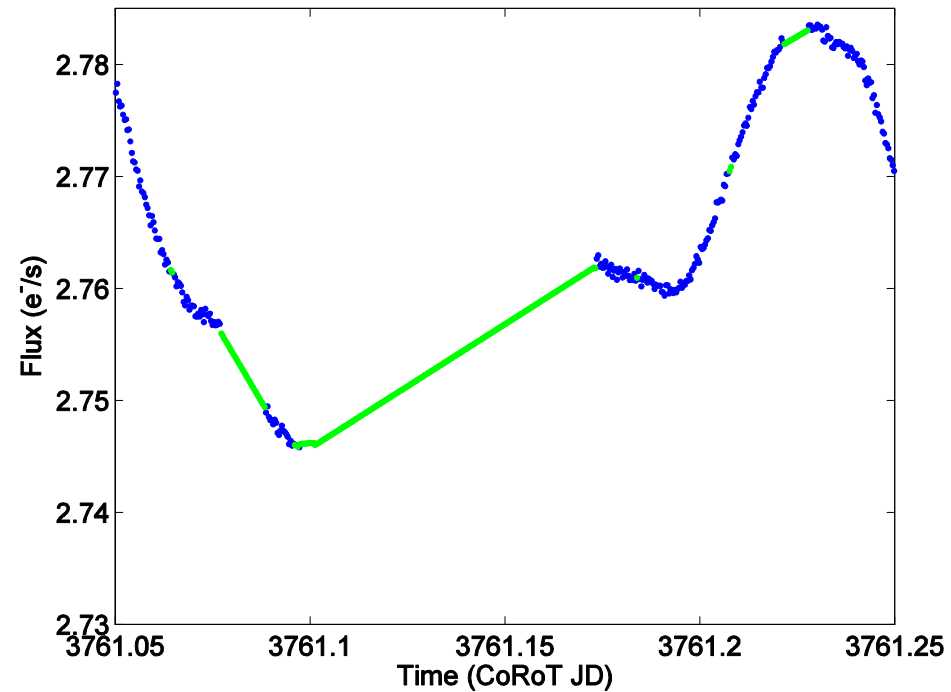
# Wrong data produced by the South Atlantic Anomaly



# INTERPOLATION: HD170699

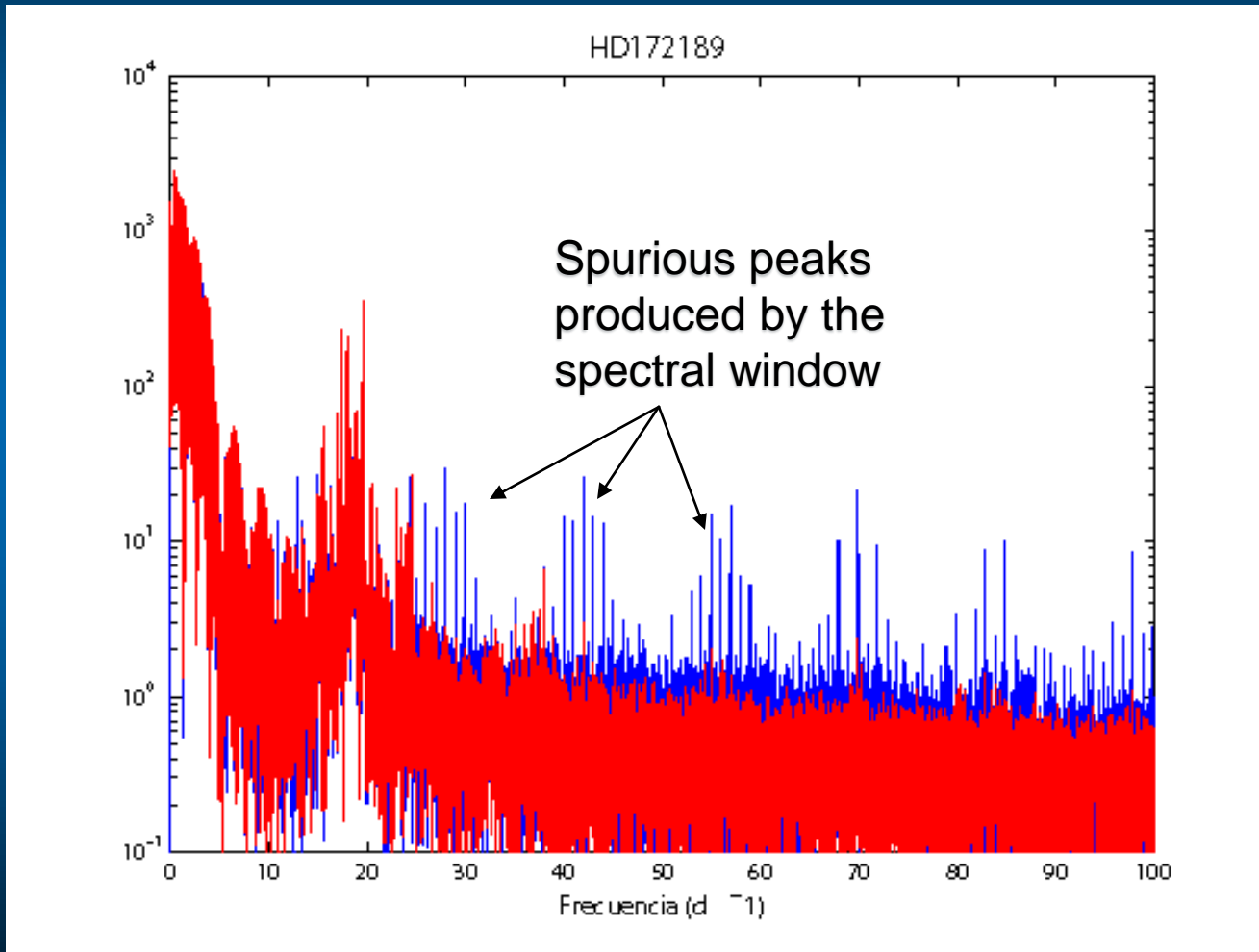


— ARMA interpolated



— Linearly interpolated

## CoRoT passing through the SAA introduce spurious peaks





# FREQUENCY DETECTION: SIGSPEC

Reegen, P. 2007, A&A, 467, pp.1353-1371

*Iterative process consisting of four steps:*

1. Computation of the significance spectrum.
2. Exact determination of the peak with maximum significance.
3. MultiSine least-squares fit of the frequencies, amplitudes and phases of all significant signal components detected so far.
4. Pre-whitening of the sinusoidal components. The residuals are used as input for the next iteration.

# COMBINATIONS FILTERING

- The procedure followed is similar to

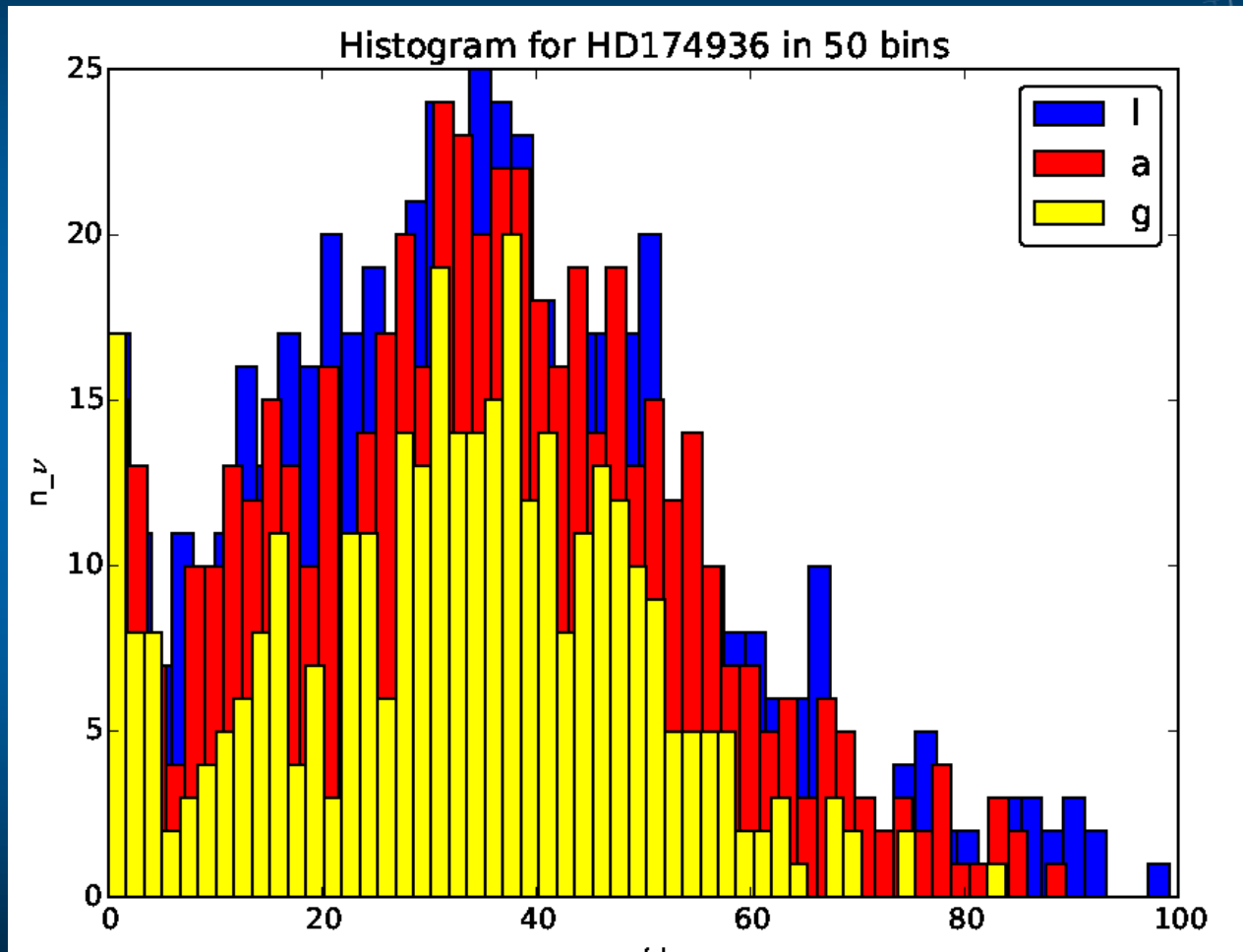
García Hernández, A., Moya, A., Michel, E. et al. 2013, A&A, A63, 14

- Independent freqs. used to find combinations with Combine from Reegen, P.

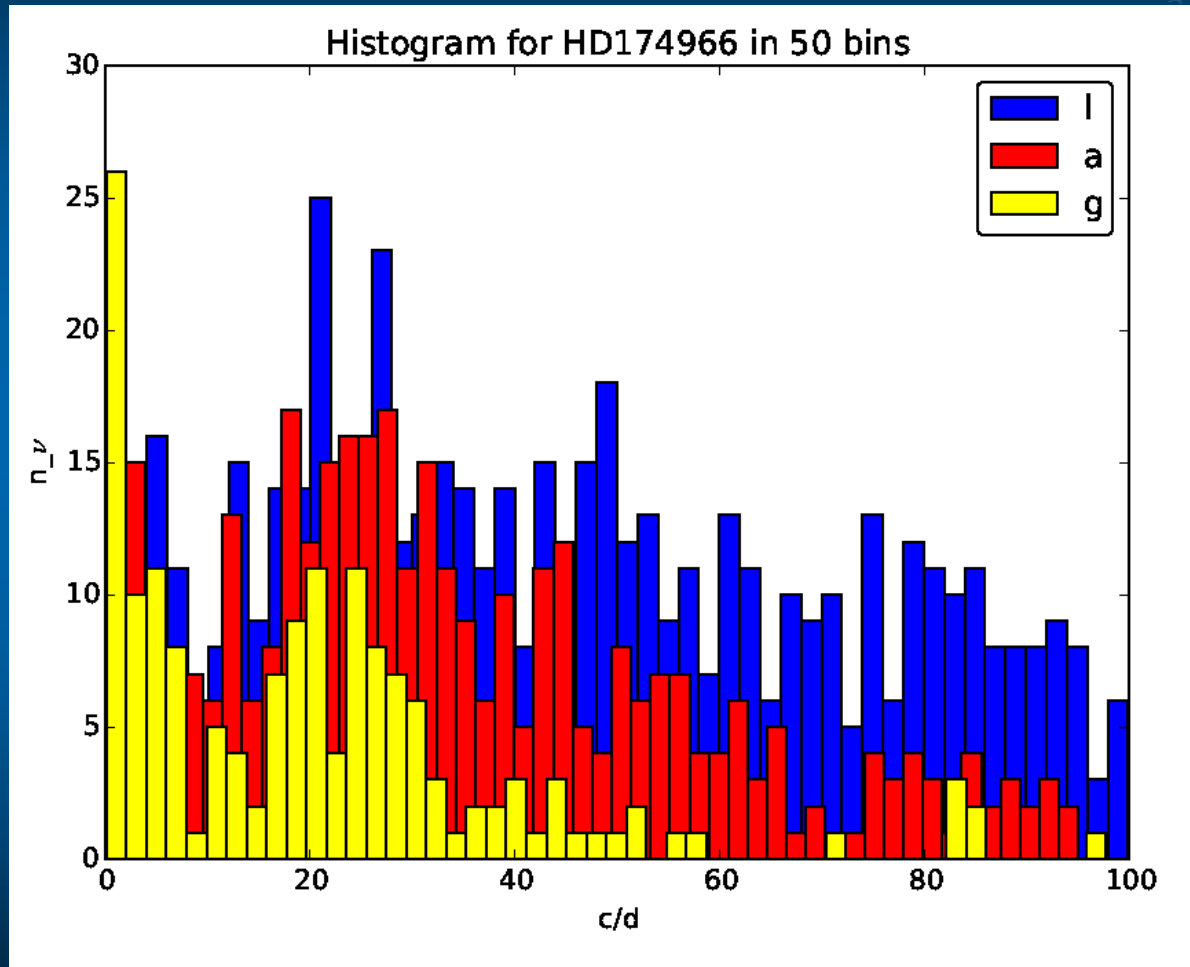
Reegen, P., 2011, CoAst, 163, p.119

- Harmonics and combinations up to 3rd order within a  $1/T_{\text{obs}}$  interval.
- A set of 12 independent freqs. Is used, harmonics until the 5th order, and combinations  $AF_a + BF_b$  being  $A, B = [1,3]$ .
- Interactions with the satellite orbital freq. ( $f_s = 13.972 \text{ d}^{-1}$ ) for F1 to F4 and the 4 first harmonics of  $f_s$ .
- Sidelobes of the  $1 \text{ d}^{-1}$  alias around  $f_s$  and its harmonics.

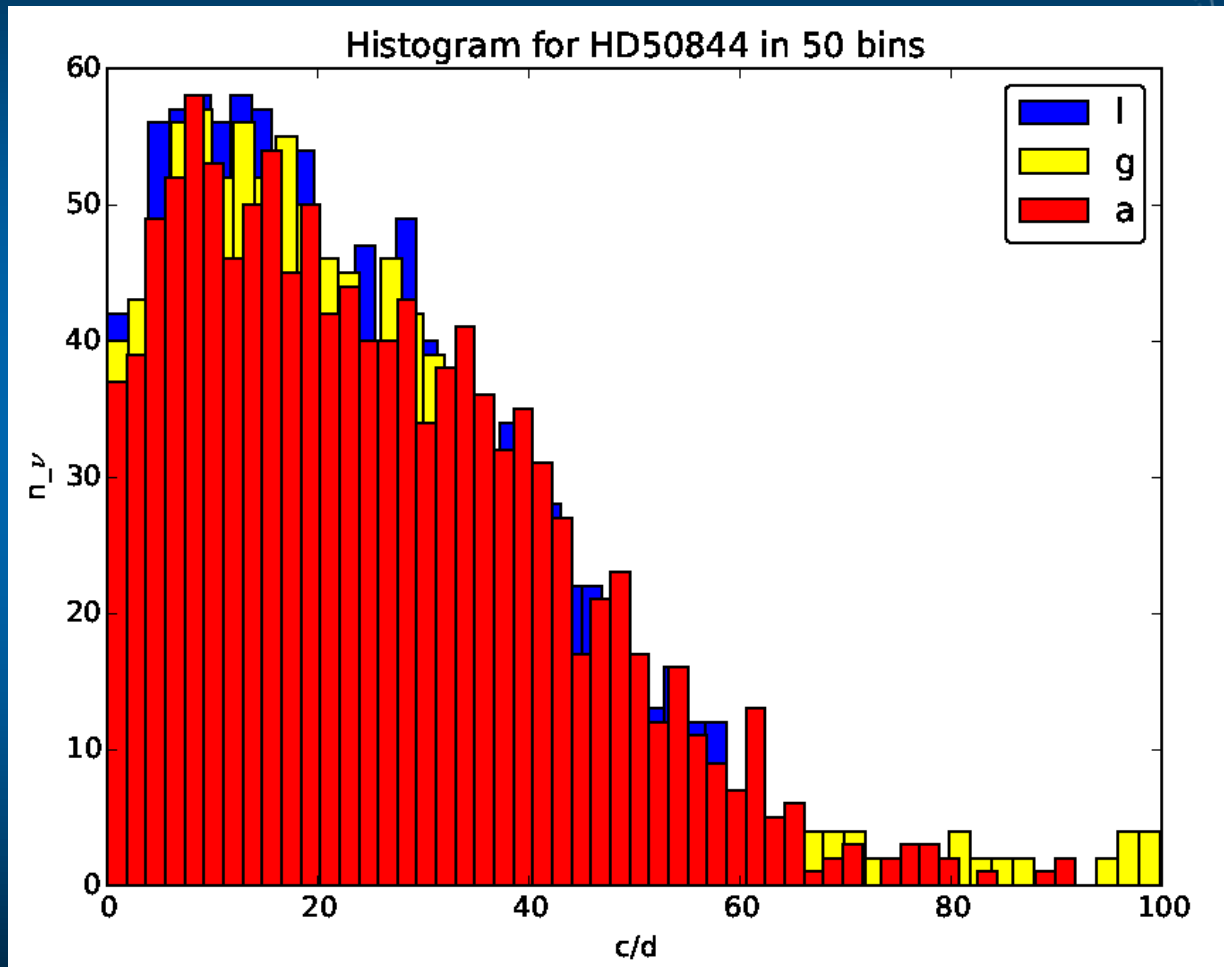
# RESULTS: HISTOGRAM OF FREQUENCIES



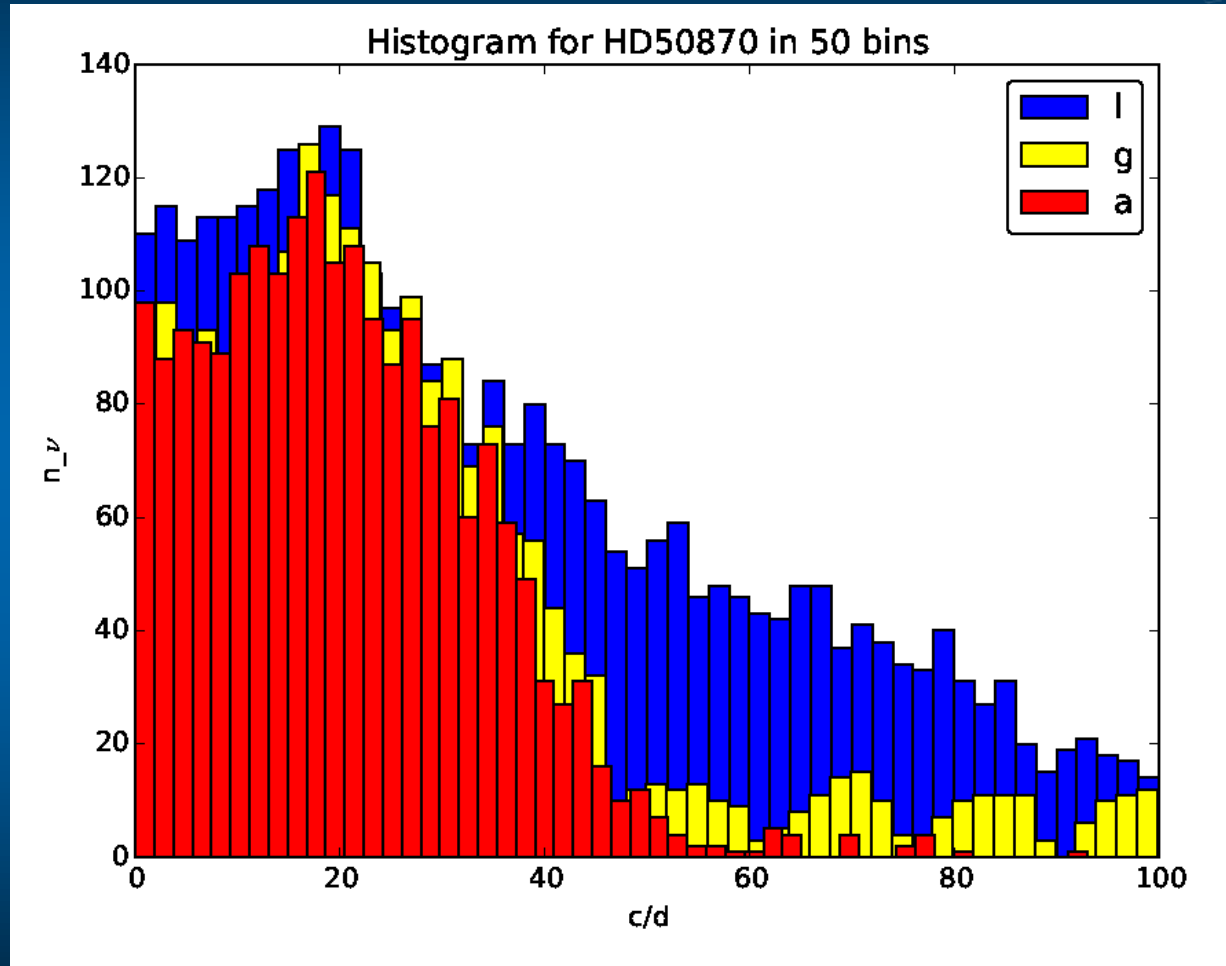
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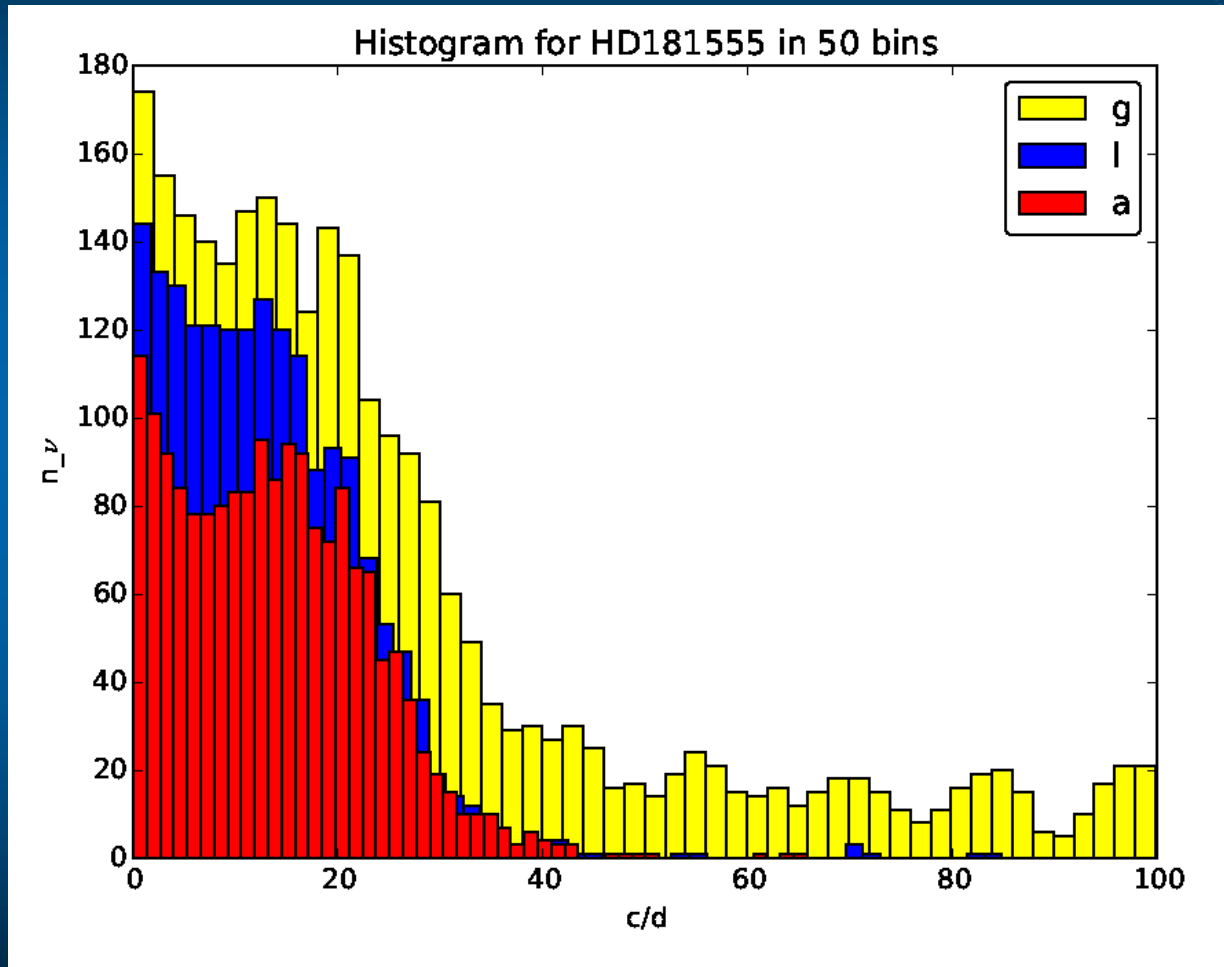
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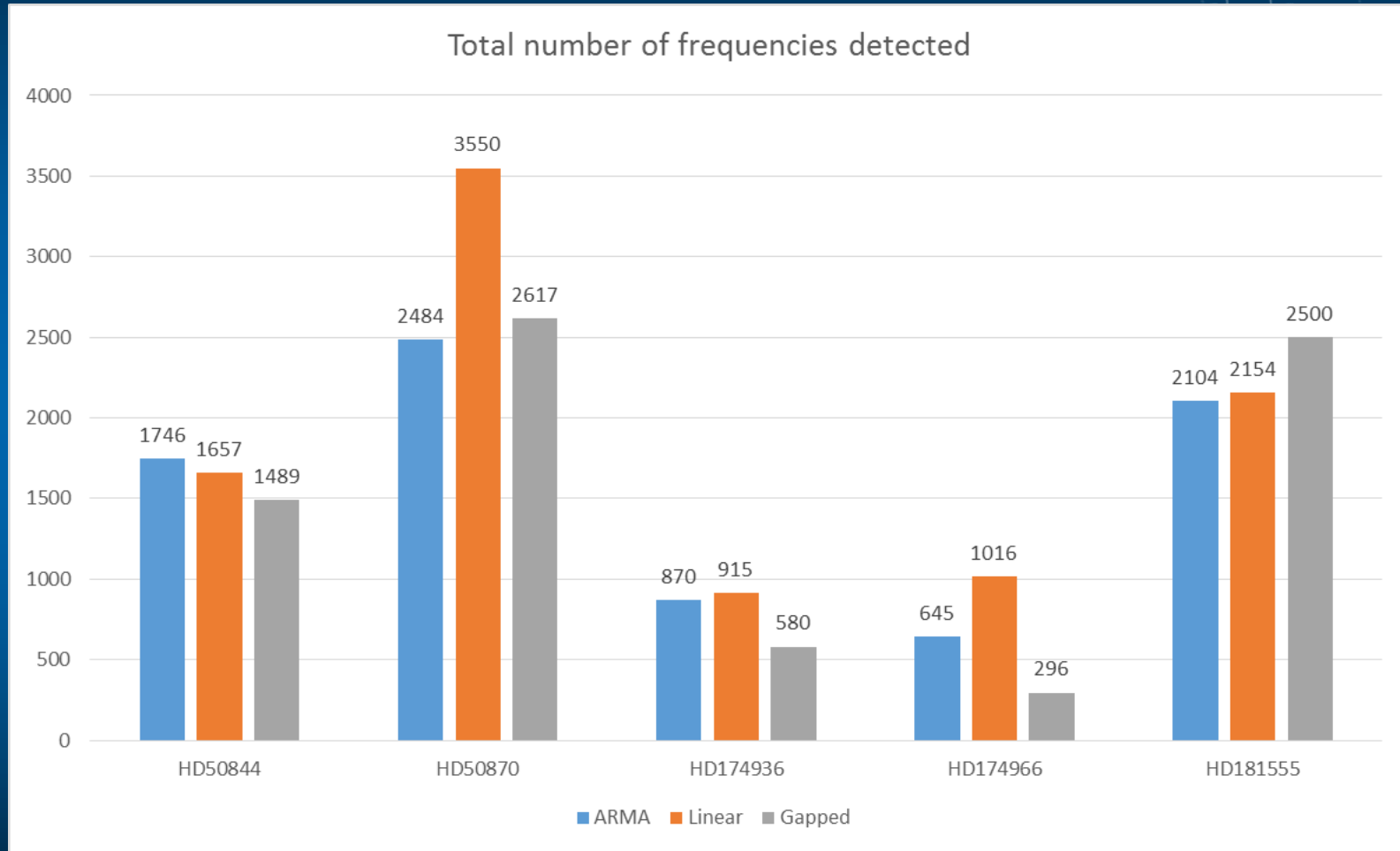
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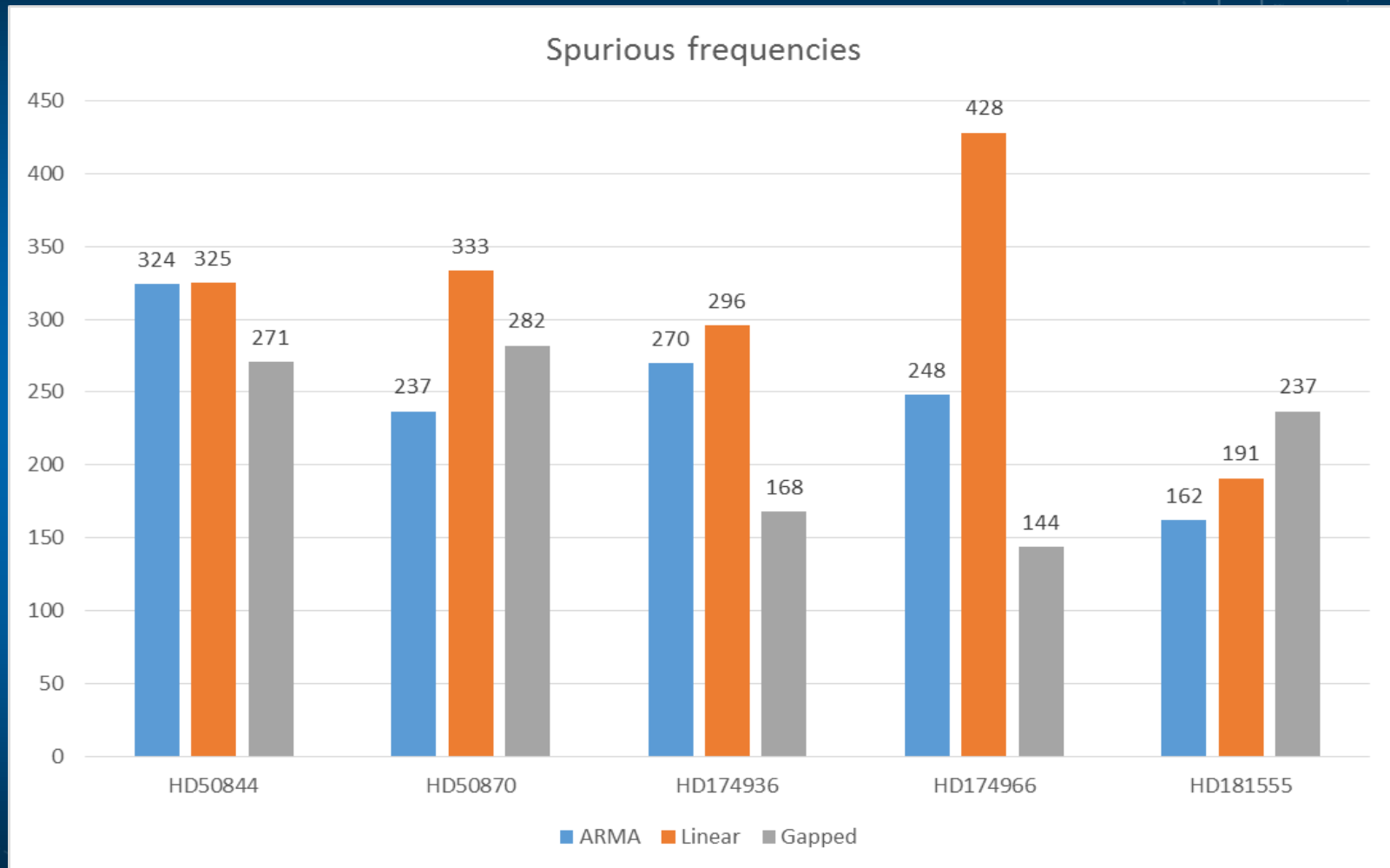


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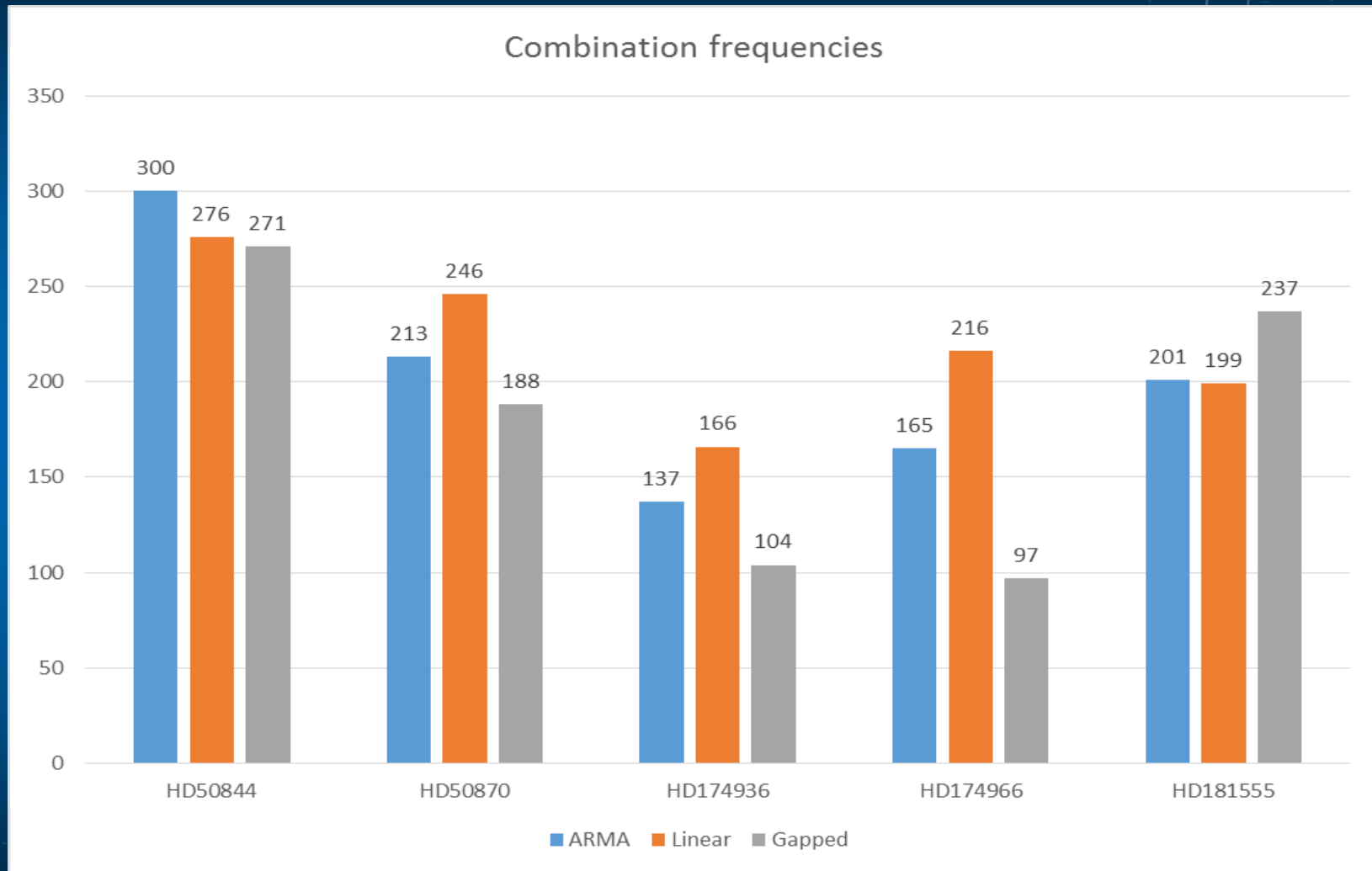




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# IN SUMMARY

Expectations from prewhitening



This is what actually happens



# CONCLUSIONS

- Prewhitening techniques (CLEAN) are not always reliable.
- An unbiased estimator of the frequency spectrum is not guaranteed when classical prewhitening techniques are used.

More info on this:

**Limits in the application of harmonic analysis to pulsating stars**

Pascual-Granado, J., Garrido, R., Suárez, J. C., 2015, A&A, 581, A89